

Chapter 2 : Polynomials

Remainder Theorem : Let $P(x)$ be any polynomial of degree greater than or equal to one and let a be any real number . If $P(x)$ is divided by the linear polynomial $x-a$ then the remainder is $P(a)$.

$$\text{Dividend} = (\text{divisor} \times \text{quotient}) + \text{remainder}$$

Factor theorem : If $P(x)$ is a polynomial of degree $n \geq 1$ and a is any real number then (i) $x-a$ is a factor of $P(x)$, if $P(a) = 0$, and (ii) $P(a) = 0$, if $x - a$ is a factor of $P(x)$.

Algebraic Identities :

1. $(X + Y)^2 = X^2 + 2XY + Y^2$

2. $(X - Y)^2 = X^2 - 2XY + Y^2$

3. $X^2 - Y^2 = (X + Y)(X - Y)$

4. $(X+A)(X+B) = X^2 + (A + B)X + AB$

5. $(X+Y+Z)^2 = X^2 + Y^2 + Z^2 + 2XY + 2YZ + 2ZX$

6. $(X + Y)^3 = X^3 + 3X^2Y + 3XY^2 + Y^3$

7. $(X - Y)^3 = X^3 - 3X^2Y + 3Y^2X - Y^3$

8. $X^3 + Y^3 = (X + Y)^3 - 3XY(X + Y)$

9. $X^3 - Y^3 = (X - Y)^3 + 3XY(X - Y)$

10. $X^3 + Y^3 + Z^3 - 3XYZ = (X + Y + Z)(X^2 + Y^2 + Z^2 - XY - YZ - ZX)$

(Do as directed)

1. Find the remainder when $x^3 - ax^2 + 6x - a$ is divided by $x-a$.

2. Is $(x + 1)$ is a factor of the polynomial $x^4 + 3x^3 + 3x^2 + x + 1$?
3. Use factor theorem to determine whether $g(x)$ is a factor of $p(x)$, where $g(x) = x + 2$ and $p(x) = x^3 + 3x^2 + 3x + 1$.
4. Find the value of K , if $(x - 1)$ is a factor of $p(x) = Kx^2 - 3x + K$.
5. Factorise : (a) $2x^2 + 7x + 3$
 (b) $x^3 - 3x^2 - 9x - 5$
6. Use suitable identity to evaluate : (a) $(x + 8)(x - 10)$
 (b) 95×96
 (c) $(998)^3$
7. Factorise the following using appropriate identities :
 (a) $9x^2 + 6xy + y^2$.
 (b) $4x^2 + 9y^2 + 16z^2 + 12xy - 24yz - 16xz$.
 (c) $27 - 125a^3 - 135a + 225a^2$.
8. Expand the following :
 (a) $(2x - y + z)^2$
 (b) $(\frac{3}{2}x + 1)^3$
9. Verify : (a) $x^3 + y^3 = (x + y)(x^2 - xy + y^2)$
 (b) $x^3 - y^3 = (x - y)(x^2 + xy + y^2)$
10. Factorise : (a) $8x^3 + y^3 + 27z^3 - 18xyz$
 (b) $27y^3 + 125z^3$
