

- The principal value of  $\sin^{-1}\left(\sin \frac{2\pi}{3}\right)$  is  
 a)  $\frac{2\pi}{3}$                       b)  $\frac{\pi}{3}$                       c)  $\frac{4\pi}{3}$                       d) None of these
- The principal value of  $\cos^{-1}\left\{\frac{1}{\sqrt{2}}\left(\cos \frac{9\pi}{10} - \sin \frac{9\pi}{10}\right)\right\}$  is  
 a)  $\frac{3\pi}{10}$                       b)  $\frac{17\pi}{20}$                       c)  $\frac{9\pi}{20}$                       d) None of these
- Let  $f : R \rightarrow R$  and  $g : R \rightarrow R$  be two functions such that  $f \circ g(x) = \sin x^2$  and  $g \circ f(x) = \sin^2 x$ , then  $f(x)$  and  $g(x)$  are  
 a)  $f(x) = x^2$  and  $g(x) = \sin x$                       b)  $f(x) = \sin x$  and  $g(x) = x^2$   
 c)  $f(x) = \sin^2 x$  and  $g(x) = \sqrt{x}$                       d)  $f(x) = \sin x$  and  $g(x) = \sqrt{x}$
- The principal value of  $\sin^{-1}\left\{\cos\left(\sin^{-1}\frac{\sqrt{3}}{2}\right)\right\}$  is  
 a)  $\frac{\pi}{6}$                       b)  $\frac{\pi}{3}$                       c)  $-\frac{\pi}{3}$                       d) None of these
- Let  $f : R \rightarrow R$  and  $g : R \rightarrow R$  be two functions such that  $f(x) = 2x - 3$  and  $g(x) = x^3 + 5$ , then  $(f \circ g)^{-1}(x)$  is equal to  
 a)  $\left(\frac{x+7}{2}\right)^{\frac{1}{3}}$                       b)  $\left(x - \frac{7}{2}\right)^{\frac{1}{3}}$                       c)  $\left(\frac{x-2}{7}\right)^{\frac{1}{3}}$                       d)  $\left(\frac{x-7}{2}\right)^{\frac{1}{3}}$
- Let  $f : R \rightarrow R$  and  $g : R \rightarrow R$  defined by  $f(x) = x + 2$  and  $g(x) = 2 - x$ , then  $(f \circ g)(3)$  is equal to  
 a) 1                      b) 2                      c) 3                      d) None of these
- The inverse of the function  $f(x) = 3x - 5$ ,  $x \in R$  is  
 a)  $\frac{1}{3x-5}$                       b)  $\frac{x+5}{3}$                       c)  $\frac{1}{3x+5}$                       d)  $\frac{1}{5x-3}$
- Let  $f : N \rightarrow R: f(x) = \frac{2x-3}{2}$  and  $g : Q \rightarrow R: g(x) = x + 2$  be two functions, then  $(f \circ g)\left(\frac{3}{2}\right)$  is  
 a) 3                      b) 1                      c)  $\frac{7}{2}$                       d) None of these
- Which of the following is the principal value branch of  $\cos^{-1} x$ ?  
 a)  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$                       b)  $(0, \pi)$                       c)  $[0, \pi]$                       d)  $(0, \pi) - \left\{\frac{\pi}{2}\right\}$

10. Which of the following is the principal value branch of  $\cos^{-1}x$  ?

- a)  $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$       b)  $(0, \pi) - \left\{\frac{\pi}{2}\right\}$       c)  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$       d)  $\left[-\frac{\pi}{2}, \frac{\pi}{2}\right] - \{0\}$

11. If  $f : [0, \infty) \rightarrow [0, \infty)$  and  $f(x) = \frac{x}{x+1}$ , then  $f$  in  $R$  is

- a) one-one and onto      b) one-one but not onto  
c) onto but not one-one      d) neither one-one nor onto

12. Let  $f : R \rightarrow R$  be a function defined by  $f(x) = x^3 + 4$ , then  $f$  is

- a) injective      b) surjective  
c) bijective      d) None of these

13. The function  $f : N \rightarrow N$ , where  $N$  is the set of natural number defined by  $f(x) = 7x + 11 \quad \forall x \in N$  is

- a) injective      b) surjective  
c) bijective      d) None of these

14. Let  $N$  be the set of natural number and the function  $f : N \rightarrow N$  defined by  $f(x) = 2x + 3 \quad \forall x \in N$ , then  $f$  is :

- a) injective      b) surjective  
c) bijective      d) None of these

15. The function  $f : N \rightarrow N$ , where  $N$  is the set of natural number defined by  $f(x) = 6 + 5x$  is :

- a) injective      b) surjective  
c) bijective      d) None of these

16. If  $f(x) = \frac{x^2 - 4}{x^2 + 4}$  for  $|x| \geq 2$ , then the  $f : (-\infty, -2) \cup [2, \infty) \rightarrow (-1, 1)$  is

- a) one-one and into      b) one-one and onto  
c) onto but not one-one      d) many-one and into

17. A function  $f$  from the set of natural number to integer

$$f(x) = \begin{cases} \frac{n-1}{2}, & \text{when } n \text{ is odd} \\ -\frac{n}{2}, & \text{when } n \text{ is even} \end{cases} \text{ is}$$

- a) one-one but not onto      b) onto but not one-one  
c) one-one and onto both      d) neither one-one nor onto

18. For all real  $x$ , let  $f(x) = x^3 + 5x + 1$ , then

- a) one-one and onto      b) onto but not one-one  
c) one-one and onto both      d) neither one-one nor onto

19. If  $\sin^{-1}x = y$ , then

- a)  $0 \leq y \leq \pi$       b)  $-\frac{\pi}{2} \leq y \leq \frac{\pi}{2}$       c)  $0 < y < \pi$       d)  $-\frac{\pi}{2} < y < \frac{\pi}{2}$

20. If  $\sin^{-1}\left(\frac{3x}{5}\right) + \sin^{-1}\left(\frac{4x}{5}\right) = \sin^{-1}x$ , then the value  $x$  is

- a) 0, 1      b) 0, -1      c) 1, -1      d) 0, 1, -1

## Activity I

To verify that the relation  $R$  in the set  $L$  of all lines in a plane, defined by  $R = \{(l, m) : l \perp m\}$  is symmetric but neither reflexive nor transitive.